

$$\begin{aligned}
& \overset{M}{H_1}(M, Z) = 0 \\
& \overset{M}{1}^{\text{description, sloped, isomorphic/.style =}} \\
& \text{arsymbol} = \cong,]H_2(M, Z) \times \\
& H_2(M, Z) \longrightarrow \\
& \mathbb{Z} \\
& \overset{M}{Y} = \\
& \partial M \\
& b_1(Y) = \\
& 0 \\
& H_1(Y, Z) \\
& H_2(M, Z) \times \\
& H_2(M, Z) \longrightarrow \\
& \mathbb{Z}H_2(M, Z) \longrightarrow \\
& (H_2(M, Z), Z) \\
& (a, b) \mapsto \\
& Za \mapsto \\
& (a,) \in \\
& H_2(M, Z) \\
& H_1(Y, Z) \\
& K \subset \\
& S^3 \\
& \tilde{X} = \\
& S^3 \setminus \\
& K \\
& X \rho X \\
& C_*(\tilde{X}) \\
& \mathbb{Z}[t, t^{-1}] \cong \\
& \mathbb{Z}[\tilde{Z}] \\
& H_1(\tilde{X}, \mathbb{Z}[t, t^{-1}]) \\
& K \\
& {}_1(\tilde{X}, \mathbb{Z}[t, t^{-1}]) \times \\
& H_1(\tilde{X}, \mathbb{Z}[t, t^{-1}]) \longrightarrow \\
& Q\mathbb{Z}[t, t^{-1}] \\
& {}_1(\tilde{X}, \mathbb{Z}[t, t^{-1}]) \cong \\
& \mathbb{Z}[t, t^{-1}]^n (tV - V^T)\mathbb{Z}[t, t^{-1}]^n, \\
& \text{where } \tilde{X} \text{ is a Seifert matrix.} \\
& {}_1(\tilde{X}, \mathbb{Z}[t, t^{-1}]) \times \\
& H_1(\tilde{X}, \mathbb{Z}[t, t^{-1}]) \longrightarrow \\
& Q\mathbb{Z}[t, t^{-1}] \\
& (\alpha, \beta) \mapsto \\
& \alpha^{-1}(t - \\
& 1)(tV - \\
& V^T)^{-1}\beta \\
& \mathbb{Z} \\
& \tilde{R} \\
& \xi \in \\
& S^1 \setminus \\
& \{\pm 1\} p_\xi = \\
& (t - \\
& \xi)(t - \\
& \xi^{-1})t^{-1} \\
& \xi \in \\
& \tilde{R} \setminus \\
& \{\pm 1\} q_\xi = \\
& (t - \\
& \xi)(t - \\
& \xi^{-1})t^{-1} \\
& \xi \notin \\
& \tilde{R} \cup \\
& S^1 q_\xi = \\
& (t - \\
& \xi)(t - \\
& \xi)(t - \\
& \xi^{-1})(t - \\
& \xi^{-1})t^{-2} \\
& \Lambda = \\
& \mathbb{Z}[t, t^{-1}] \\
& {}_1(X, \Lambda) \cong \\
& \bigoplus_{\xi \in S^1 \setminus \{\pm 1\}} \bigoplus_{k \geq 0} (\Lambda p_\xi^k)^{n_k, \xi} \oplus \\
& \bigoplus_{\xi \notin S^1} \bigoplus_{l \geq 0} (\Lambda q_\xi^l)^{n_l, \xi}
\end{aligned}$$

On
isome-
tries